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Theoretical study of the reaction of CH_2XO (X = F, Cl, Br) radicals with the NO radical

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Abstract In this paper, we focus on the multiple-channel reactions of CH_2XO (X = F, Cl, Br) radicals with the NO radical by means of direct dynamic methods. All structures of the stationary points were obtained at the MP2/6-311+G(d,p) level and vibrational frequency analysis was also performed at this level of theory. The minimum energy path (MEP) was obtained via the intrinsic reaction coordinate (IRC) theory at the MP2/6-311+G(d,p) level, and higher-level energetic information was refined by the MC-QCISD method. The rate constants for the three hydrogen abstraction reaction channels over the temperature range 200-1,500 K were calculated by the improved canonical variational transition state theory (ICVT) with a correction for small-curvature tunneling (SCT). The rate constants calculated in this manner were in good agreement with the available experimental data, and the threeparameter rate-temperature formulae for the temperature

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Key Laboratory of Cluster Science of Ministry of Education & School of Chemistry, Beijing Institute of Technology, Beijing 100081, People's Republic of China range 200–1,500 K were $k_{1a}(T) = 0.32 \times 10^{-18} T^{1.83} \exp(1748.54/T), k_{2a}(T) = 0.22 \times 10^{-19} T^{2.19} \exp(1770.19/T), k_{3a}(T) = 0.88 \times 10^{-20} T^{2.20} \exp(1513.82/T)$ (in units of cm³ molecule⁻¹s⁻¹).

Keywords Gas-phase reaction · Transition state · Rate constants

Introduction

Halogen-containing compounds are important products of the incineration of municipal waste [1], as well as significant atmospheric pollutants. Halogen-substituted alkoxy radicals are known to be important intermediates in the combustion of halogen-containing compounds [2–4]. In the atmosphere, a halogen-substituted alkoxy radical CH₂XO (X = F, Cl, Br) can react with an NO radical, leading to the abstraction of either an H atom or the halogen atom from the CH₂XO (X = F, Cl, Br) radical. We therefore have six feasible reaction pathways for the title reaction (denoted R1a, R1b, R2a, R2b, R3a, R3b, respectively), as follows:

$NO + CH_2FO \rightarrow CHFO + HNO$	(R1a)
\rightarrow CH ₂ O + FNO	(R1b)
$NO + CH_2ClO \rightarrow CHClO + HNO$	(R2a)
\rightarrow CH ₂ O + ClNO	(R2b)
$NO + CH_2BrO \rightarrow CHBrO + HNO$	(R3a)
\rightarrow CH ₂ O + BrNO	(R3b)

In 2001, F. X. Wu and R. W. Carr [3] obtained the rate constants for the reaction NO + CH₂ClO \rightarrow CHClO + HNO (R2a) over the temperature range 265–306 K by UV flash photolysis with time-resolved mass spectrometry. The experimental value at 289 K was $(2.70\pm0.4)\times10^{-12}$ cm³mole-cule⁻¹s⁻¹.

For the title reactions, experimental measurements were performed in the low-temperature range, and no experimental data are available for the high-temperature range. However, the rate constant must be evaluated at high temperatures if we are to gain a deeper understanding of the mechanism of this multiple-channel reaction. Consequently, it is necessary to calculate the rate constant at high temperatures theoretically. To the best of our knowledge, no previous theoretical work on the kinetics of the title reactions has been reported.

In the work described in this paper, the kinetics of the reactions of CH_2XO (X = F, Cl, Br) radicals with the NO radical were studied using a dual-level direct dynamics method [5-9]. The potential energy surface information (geometries, energies, gradients, force constants) of all the stationary points (reactants, complexes, products, and transition states) and 16 points (eight points in the reactant channel, eight points in the product channel) selected along the minimum energy path (MEP) of each reaction channel were obtained directly from electronic structure calculations at the MP2/6-311+G(d,p)level. Complex energies corrected for basis set superposition error (BSSE) were further confirmed by the standard counterpoise method of Boys and Bernardi [10]. Higher-level singlepoint energy corrections were performed by the MC-QCISD method [11]. Subsequently, the POLYRATE 9.7 program [12] was employed to calculate the rate constants of the three hydrogen abstraction reaction channels by the variational transition state theory (VTST) [13, 14] proposed by Truhlar and coworkers. Theoretical and experimental results were then compared. Our results may prove useful in further experimental investigations.

Computational methods

In the present work, we optimized the equilibrium geometries and vibrational frequencies of all of the stationary points (reactants, complexes, products, and transition states) at the restricted or unrestricted second-order Møller-Plesset perturbation (MP2) [15–18] level with the 6-311+G(d,p) basis set. Complex energies were further confirmed with BSSE correction. Using intrinsic reaction coordinate (IRC) theory, the MEP was obtained with a gradient step size of $0.05 \text{ (amu)}^{1/2}$ bohr at the MP2/6-311+G(d,p) level. The first and second derivatives of the energy were then obtained to calculate the curvature of the reaction path and the generalized vibrational frequencies along the reaction path. The MC-QCISD method (multi-coefficient correlation method based on quadratic configuration interaction with single and double excitations, proposed by Fast and Truhlar) [11] was employed to refine the energy information in order to get more accurate energies and barrier heights, based on the MP2/6-311+G(d,p) geometries. All of the calculations were performed using the GAUSSIAN 03 software package [19].

VTST [13, 14] was used to calculate the rate constants in the program POLYRATE 9.7 [12]. The theoretical rate constants for the three hydrogen abstraction reaction channels over the temperature range 200–1,500 K were calculated using the improved canonical variational transition state theory (ICVT) [20] with the small-curvature tunneling (SCT) [21] correction proposed by Truhlar and coworkers [20]. For the three reaction channels, all of the vibrational modes were treated as separable quantum harmonic oscillators. The curvature components were calculated using a quadratic fit to obtain the derivative of the gradient with respect to the reaction coordinate.

Results and discussions

Stationary points

The optimized structures of the reactants (CH₂FO, CH₂ClO, CH₂BrO, and NO), complexes (CR1a, CR2a, and CR3a), products (CHFO, CHClO, CHBrO, HNO, FNO, ClNO, BrNO, and CH₂O), and transition states (TS1a, TS1b, TS2a, TS2b, TS3a, and TS3b) calculated at the MP2/6-311+G(d,p)level are depicted in Fig. 1, along with the available experimental values [22, 23]. The theoretical geometric parameters of NO, HNO, CHFO, CH₂O, FNO, and CINO are in good agreement with the corresponding experimental values [22, 23]. In Fig. 1, all of the transition states have the same symmetry, C_1 . In the structures TS1a, TS2a, and TS3a, the C—H bond that breaks is elongated by 23 %, 23 %, and 26 % compared to the equilibrium bond lengths in CH₂FO, CH₂ClO, and CH₂BrO, respectively; the resulting N-H bond is stretched by 33 %, 30 %, and 31 % compared to the equilibrium bond length in isolated HNO, respectively. Thus, the elongation of the breaking C-H bond is smaller than the elongation of the resulting N-H bond. Similarly, for the structures TS1b, TS2b, and TS3b, the breaking bonds are again less elongated than the resulting bonds, indicating that the abovementioned reaction channels are all reactant-like (i.e., the six reaction channels proceed via "early" transition states, which is consistent with Hammond's postulate [24] for an exothermic reaction).

The harmonic vibrational frequencies of the stationary points (including the reactants, complexes, products, and transition states) obtained at the MP2/6-311+G(d,p) level as well as the experimental values available [25–27] are presented in Table 1. It is obvious that the calculated frequencies for the species HNO, CHClO, and CH₂O are in agreement with their corresponding experimental values, with the largest deviation being <9 %. The six transition states were all confirmed by normal-mode analysis as having one and only one imaginary frequency, which corresponds to the stretching mode for coupling between the breaking and forming bonds.



Fig. 1 Optimized geometries of the reactants, products, complexes, and transition states calculated at the MP2/6-311+G(d,p) level. The *values in parentheses* are the experimental values (obtained from [22,

23] for NO, HNO, CHFO, FNO, ClNO, and CH_2O , respectively). Bond lengths are in angstroms and angles are in degrees

Species	Value(s) calculated via MP2/6-311+G(d,p)	Experimentally determined values
NO	3553	
CH ₂ FO	3090, 3028, 1425, 1411, 1212, 1143, 1035, 845, 556	
CH ₂ ClO	3049, 3110, 1381, 1368, 1121, 1111, 750, 710, 415	
CH ₂ BrO	3118, 3052, 1383, 1309, 1111, 1050, 641, 631, 335	
HNO	3035, 1582, 1500	2756, 1563,1511 ^a
CHFO	3166, 1860, 1397, 1063, 1043, 662	
CHClO	3112, 1793, 1386, 970, 769, 473	2929, 1784, 1307, 932, 739, 457 ^b
CHBrO	3098, 1795, 1344, 926, 661, 369	
CH ₂ O	3049, 2977, 1762, 1558, 1278, 1205	2843, 2782, 1746, 1500, 1249, 1167 ^c
FNO	1937, 712, 441	
CINO	1892, 579, 313	
BrNO	1896, 531, 261	
CR1a	3077, 2285, 1899, 1509, 1380, 1315, 1263, 1020, 935, 641, 553, 401, 373, 248, 126	
CR2a	3091, 2303, 1899, 1498, 1334, 1287, 1236, 938, 683, 622, 423, 400, 372, 237, 96	
CR3a	3097, 2291, 1875, 1505, 1334, 1239, 1208, 888, 635, 579, 420, 389, 301, 226, 76	
TS1a	3048, 1860, 1576, 1472, 1362, 1297, 1202, 984, 718, 586, 392, 285, 205, 144, 1041 <i>i</i>	
TS1b	3174, 3078, 1604, 1520, 1364, 1247, 1214, 1104, 512, 358, 213, 152, 96, 21, 1194 <i>i</i>	
TS2a	3044, 1858, 1555, 1480, 1324, 1285, 1109, 711, 697, 423, 349, 256, 256, 181, 108, 977 <i>i</i>	
TS2b	3133, 3052, 1807, 1553, 1335, 1237, 1120, 1001, 368, 320, 193, 123, 68, 29, 705 <i>i</i>	
TS3a	3044, 1864, 1578, 1488, 1283, 1265, 1058, 688, 604, 368, 300, 249, 161, 88, 757 <i>i</i>	
TS3b	3125, 3045, 1885, 1549, 1304, 1233, 1020, 936, 312, 248, 145, 95, 60, 7, 549 <i>i</i>	

Table 1 Calculated and experimental frequencies (in cm^{-1}) for the reactants, complexes, products, and transition states for the title reactions, calculated at the MP2/6-311+G(d,p) level

^a From [25]

^b From [26]

^c From [27]

Energetics

Table 2 lists the reaction enthalpies (ΔH_{298}^0) and potential barrier heights (ΔE^{TS}) , including zero-point energy (ZPE) corrections, for the six reaction channels, calculated at the MC-QCISD//MP2/6-311+G(d,p) level. From Table 2, it is apparent that the six individual reaction channels are all exothermic, which is consistent with Hammond's postulate [24] discussed above.

Potential energy diagrams for the reactions NO + CH₂FO \rightarrow products, NO + CH₂ClO \rightarrow products, and NO + CH₂BrO \rightarrow products, including ZPE corrections calculated at the MC-QCISD//MP2/6-311+G(d,p) level, are plotted in Figs. 2, 3, and 4, respectively. To facilitate comparisons, the energies of the reactants are set to zero. For the complexes CR1a, Cr2a, and CR3a, the energies were calculated to be -37.63, -49.43, and -53.08 kJ mol⁻¹, respectively, at the MC-QCISD//MP2/6-311+G(d,p) level. The energies of the complexes are close to those of the reactants, and it is unclear whether the complexes really do exist. According to the BSSE-corrected results obtained at the MP2/6-311+G(d,p) level, the relative energies of the complexes CR1a, Cr2a,

and CR3a are -100.94, -110.68, and -118.21 kJ mol-1. respectively. The energies of these complexes are much lower than the reactants, which means that these weakly bonded complexes exist. For the six reaction channels, the potential barrier heights for the reaction channels R1a, R2a, and R3a are lower than those for R1b, R2b, and R3b by 169.02, 111.51, and 105.23 kJ mol^{-1} when calculated at the MC-QCISD//MP2/6-311+G(d,p) level, respectively. At the same time, the reaction channels R1a, R2a, and R3a are more exothermic than R1b, R2b, and R3b by about 83.22, 30.43, and 11.51 kJ mol⁻¹, respectively. As a result, R1a, R2a, and R3a are more thermodynamically and kinetically favorable than R1b, R2b, and R3b, indicating that R1a, R2a, and R3a are the major reaction channels whereas paths R1b, R2b, and R3b are only very rarely used. Thus, we only calculated the rate constants for the three hydrogen abstraction reaction channels R1a, R2a, and R3a.

Rate constants

Dual-level dynamics calculations [5–9] of R1a, R2a, and R3a were carried out at the MC-QCISD//MP2/6-311+G(d,p)

Table 2 The reaction enthalpies at 298 K (ΔH_{298}^0) and the barrier heights (ΔE^{TS}) (kJ mol⁻¹) with zero-point energy (ZPE) corrections for the reactions of CH₂XO (X = F, Cl, Br) radicals with the NO radical, calculated at the MC-QCISD//MP2/6-311+G(d,p) level

Parameter calculated	Reaction channel	MC-QCISE //MP2
ΔH_{298}^{0}	$NO + CH_2FO \rightarrow CHFO + HNO (R1a)$	-181.88
	$NO + CH_2FO \rightarrow CH_2O + FNO (R1b)$	-98.66
	$NO + CH_2CIO \rightarrow CHCIO + HNO (R2a)$	-170.87
	$NO + CH_2ClO \rightarrow CH_2O + ClNO (R2b)$	-140.44
	$NO + CH_2BrO \rightarrow CHBrO + HNO (R3a)$	-166.72
	$NO + CH_2BrO \rightarrow CH_2O + BrNO (R3b)$	-155.21
ΔE^{TS} +ZPE	$NO + CH_2FO \rightarrow CHFO + HNO (R1a)$	-21.22
	$NO + CH_2FO \rightarrow CH_2O + FNO (R1b)$	147.80
	$NO + CH_2CIO \rightarrow CHCIO + HNO (R2a)$	-30.47
	$NO + CH_2ClO \rightarrow CH_2O + ClNO (R2b)$	81.04
	$NO + CH_2BrO \rightarrow CHBrO + HNO (R3a)$	-32.06
	$NO + CH_2BrO \rightarrow CH_2O + BrNO (R3b)$	73.17

level. The rate constants of the three hydrogen abstraction reaction channels, k_{1a} , k_{2a} , and k_{3a} , were evaluated by conventional transition state theory (TST), improved canonical variational transition state theory (ICVT), and ICVT with the small-curvature tunneling (SCT) correction in a wide temperature range (200-1,500 K). The ICVT/SCT rate constants k_{1a} , k_{2a} , and k_{3a} are plotted against the reciprocal of temperature in Fig. 5 and are given in Table 3 along with experimental results [3]. The theoretically calculated rate constant values of k_{2a} are in good agreement with these experimental values [3]. For example, the ratio $k_{\text{ICVT/SCT}}$ k_{exptl} is 1.25, 1.12, 0.96, and 0.88 at 265, 280, 289, and 306 K, respectively. The theoretical ICVT/SCT rate constant for the reaction channel NO + $CH_2CIO \rightarrow CHCIO + HNO$ (R2a) is 2.32×10^{-12} cm³ molecule⁻¹ s⁻¹, which is lower than that $(4.09 \times 10^{-12} \text{ cm}^3 \text{ molecule}^{-1} \text{ s}^{-1})$ for the reaction channel NO + $CH_2FO \rightarrow CHFO + HNO$ (R1a) but higher than



Fig. 2 Potential energy surface for the reaction NO + CH_2FO . Relative energies (in kJ mol⁻¹) were calculated at the MC-QCISD//MP2/6-311 +G(d,p) + ZPE level



Fig. 3 Potential energy surface for the reaction NO + CH_2CIO . Relative energies (kJ mol⁻¹) were calculated at the MC-QCISD//MP2/6-311+G(d,p) + ZPE level

that $(4.11 \times 10^{-13} \text{ cm}^3 \text{ molecule}^{-1} \text{ s}^{-1})$ for the reaction channel NO + CH₂BrO \rightarrow CHBrO + HNO (R3a) at 298 K. The theoretical activation energy (E_a) was estimated based on the calculated ICVT/SCT rate constants, and it was found that the corresponding E_a value for reaction channel R2a ($-5.40 \text{ kJ mol}^{-1}$) is higher than that for reaction channel R1a (7.24 kJ mol^{-1}) but lower than that for reaction channel R3a ($-5.02 \text{ kJ mol}^{-1}$) in 350–600 K, which is in accord with its kinetic superiority. These results are consistent with the qualitative assessment based on potential energy barrier heights.

Because experimental knowledge of the title reactions is limited, we hope that our research into the kinetics of the title reactions may provide useful information for future laboratory investigations. In order to provide more convenient reference data for future experimental measurements, three-parameter fits of the ICVT/SCT rate constants for the three hydrogen abstraction reaction channels over the temperature range 200–1,500 K were performed, and the resulting expressions are given below (in units of cm³ molecule⁻¹s⁻¹):



Fig. 4 Potential energy surface for the reaction $NO + CH_2BrO$. Relative energies (in kJ mol⁻¹) were calculated at the MC-QCISD//MP2/6-311+G(d,p) + ZPE level



Fig. 5 ICVT/SCT rate constants calculated at the MC-QCISD//MP2/ 6-311+G(d,p) level for the three hydrogen abstraction reaction channel rate constants k_{1a} , k_{2a} , and k_{3a} (in cm³ molecule⁻¹s⁻¹) plotted against 1000/*T* (where *T* is between 200 and 1,500 K)

$$\begin{split} k_{1a}(T) &= 0.32 \times 10^{-18} T^{1.83} \exp(1748.54/T) \\ k_{2a}(T) &= 0.22 \times 10^{-19} T^{2.19} \exp(1770.19/T) \\ k_{3a}(T) &= 0.88 \times 10^{-20} T^{2.20} \exp(1513.82/T) \end{split}$$

Conclusions

In this work, the multi-channel reactions NO + CH_2XO (X = F, Cl, Br) were investigated theoretically. Performing

Table 3 Calculated ICVT/SCT rate constants (cm³ molecule⁻¹ s⁻¹) for reaction channels R1a, k_{1a} , R2a, k_{2a} , and R3a, k_{3a} in the temperature range 200–1,500 K, as calculated at the MC-QCISD// MP2/6-311+G(d,p) level calculations at the MP2/6-311+G(d,p) level, we obtained potential energy surface data, and the energies of the stationary points and a few extra points along the minimum energy path were refined at the MC-QCISD level. Six reaction channels were identified for the title reactions. By comparing barrier heights and performing a molecular electrostatic potential analysis, the hydrogen abstraction reaction channels were identified as the major pathways. The difference between the transition state energy and the corresponding complex energy for the reaction channel increases in the order $R_{1a} < R_{2a} < R_{3a}$. The rate constants for the three major reaction channels were calculated by ICVT with the SCT correction at the MC-QCISD//MP2/6-311+G(d,p) level. The calculated results show that the values of the ICVT/SCT rate constants decrease as the size of the halogen atom increases, in the order $k_{1a}(\text{ICVT/SCT}) > k_{2a}(\text{ICVT/SCT}) > k_{3a}(\text{ICVT/}$ SCT). The values of the ICVT/SCT rate constant k_{2a} are in good agreement with the corresponding experimental values available. The three-parameter rate-temperature formulae for the three hydrogen abstraction reaction channels were fitted with the following expressions (in cm^3 molecule⁻¹s⁻¹) in the temperature range 200-1,500 K:

 $k_{1a}(T) = 0.32 \times 10^{-18} T^{1.83} \exp(1748.54/T)$ $k_{2a}(T) = 0.22 \times 10^{-19} T^{2.19} \exp(1770.19/T)$

$$k_{3a}(T) = 0.88 \times 10^{-20} T^{2.20} \exp(1513.82/T)$$

<i>T</i> (K)	$k_{1a}(ICVT/SCT)$	$k_{2a}(ICVT/SCT)$	Experimental k values from [3]	$k_{3a}(\text{ICVT/SCT})$
200.00	2.86×10^{-11}	1.50×10^{-11}		1.78×10^{-12}
235.00	1.18×10^{-11}	6.36×10^{-12}		9.01×10^{-13}
265.00	6.68×10^{-12}	3.69×10^{-12}	2.96×10^{-12}	5.87×10^{-13}
280.00	5.26×10^{-12}	2.94×10^{-12}	2.63×10^{-12}	4.93×10^{-13}
289.00	4.62×10^{-12}	2.60×10^{-12}	$(2.7\pm0.4)\times10^{-12}$	4.48×10^{-13}
298.00	4.09×10^{-12}	2.32×10^{-12}		4.11×10^{-13}
306.00	3.69×10^{-12}	2.11×10^{-12}	2.41×10^{-12}	3.82×10^{-13}
350.00	2.30×10^{-12}	1.37×10^{-12}		2.75×10^{-13}
400.00	1.55×10^{-12}	9.58×10^{-13}		2.12×10^{-13}
450.00	1.15×10^{-12}	7.43×10^{-13}		1.78×10^{-13}
500.00	9.27×10^{-13}	6.19×10^{-13}		1.57×10^{-13}
600.00	6.96×10^{-13}	4.96×10^{-13}		1.38×10^{-13}
650.00	6.35×10^{-13}	4.66×10^{-13}		1.35×10^{-13}
700.00	5.95×10^{-13}	4.49×10^{-13}		1.34×10^{-13}
750.00	5.69×10^{-13}	4.40×10^{-13}		1.34×10^{-13}
800.00	5.53×10^{-13}	4.37×10^{-13}		1.36×10^{-13}
900.00	5.42×10^{-13}	4.46×10^{-13}		1.44×10^{-13}
1000.00	5.52×10^{-13}	4.69×10^{-13}		1.56×10^{-13}
1300.00	6.53×10^{-13}	5.97×10^{-13}		2.08×10^{-13}
1500.00	7.65×10^{-13}	7.21×10^{-13}		2.57×10^{-13}

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